

## Numerical Solutions to Schrodinger's Equation for the Particle in the Semi-infinite Box

Parameters go here:  $x_{\min} := 0$   $x_{\max} := 5$   $m := 1$   $V_0 := 2$   $lb := 2$

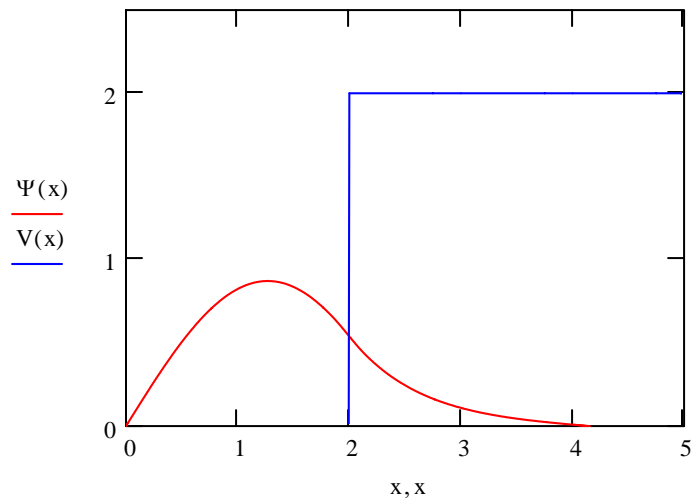
Potential energy  $V(x) := \text{if}[(x \geq lb), V_0, 0]$

Given  $\frac{d^2}{dx^2} \Psi(x) = 2 \cdot m \cdot (V(x) - E) \cdot \Psi(x)$   $\Psi(x_{\min}) = 0$   $\Psi'(0) = 0.1$

$\Psi := \text{Odesolve}(x, x_{\max})$

$$\Psi(x) := \frac{\Psi(x)}{\sqrt{\int_{x_{\min}}^{x_{\max}} \Psi(x)^2 dx}}$$

Enter energy guess:  $E \equiv 0.766$



Calculate the probability that the particle is in the barrier:

$$\int_2^5 \Psi(x)^2 dx = 0.092$$

Calculate the probability that the particle is not in the barrier:

$$\int_0^2 \Psi(x)^2 dx = 0.908$$

Calculate and display momentum distribution:

Fourier transform:

$$p := -10, -9.9 .. 10$$

$$\Phi(p) := \int_{-x_{\min}}^{x_{\max}} \exp(-i \cdot p \cdot x) \cdot \Psi(x) dx$$

