

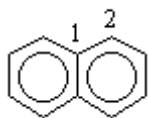
What Does Huckel MOT Have to Say About the Stability of the C₁₀H₈ Isomers?

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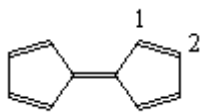
The numeric version of the Huckel molecular orbital theory (HMOT) is based on a connectivity matrix which records which atoms are bonded to each other. The eigenvalues of this matrix provide the HMOT energy levels and the HMOT wave functions.

The purpose of this exercise is to see what HMOT has to say about the relative stability of the C₁₀H₈ isomers shown below.

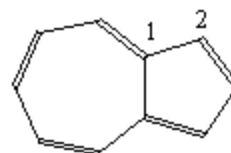
Napthalene



Fulvalene



Azulene



Napthalene calculation: Natoms := 10 Nocc := 5

$$H := \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}$$

Calculate the eigenvalues and eigenvectors: $E := \text{eigenvals}(H)$ $E := \text{sort}(E)$

$$E^T = (-2.303 \quad -1.618 \quad -1.303 \quad -1 \quad -0.618 \quad 0.618 \quad 1 \quad 1.303 \quad 1.618 \quad 2.303)$$

Calculate total π -electronic energy: $E_\pi := 2 \cdot \sum_{i=1}^{\text{Nocc}} E_i$ $E_\pi = -13.683$

Calculate the delocalization energy: $E_{\text{deloc}} := E_\pi + 2 \cdot \text{Nocc}$ $E_{\text{deloc}} = -3.683$

Calculate the delocalization energy per atom: $\frac{E_{\text{deloc}}}{\text{Natoms}} = -0.368$

Fulvalene calculation:

$$H := \begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 \end{pmatrix}$$

Calculate the eigenvalues and eigenvectors: $E := \text{eigenvals}(H)$ $E := \text{sort}(E)$

$$E^T = (-2.115 \quad -1.618 \quad -1.618 \quad -1.303 \quad 0.254 \quad 0.618 \quad 0.618 \quad 1 \quad 1.861 \quad 2.303)$$

Calculate total π -electronic energy:

$$E_{\pi} := 2 \cdot \sum_{i=1}^{\text{Nocc}} E_i \quad E_{\pi} = -12.799$$

Calculate the delocalization energy:

$$E_{\text{deloc}} := E_{\pi} + 2 \cdot \text{Nocc} \quad E_{\text{deloc}} = -2.799$$

Calculate the delocalization energy per atom:

$$\frac{E_{\text{deloc}}}{\text{Natoms}} = -0.28$$

Azulene calculation:

$$H := \begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}$$

Calculate the eigenvalues and eigenvectors: $E := \text{eigenvals}(H)$ $E := \text{sort}(E)$

$$E^T = (-2.095 \quad -1.869 \quad -1.579 \quad -0.738 \quad -0.4 \quad 0.477 \quad 0.887 \quad 1.356 \quad 1.652 \quad 2.31)$$

Calculate total π -electronic energy: $E_\pi := 2 \cdot \sum_{i=1}^{\text{Nocc}} E_i$ $E_\pi = -13.364$

Calculate the delocalization energy: $E_{\text{deloc}} := E_\pi + 2 \cdot \text{Nocc}$ $E_{\text{deloc}} = -3.364$

Calculate the delocalization energy per atom: $\frac{E_{\text{deloc}}}{\text{Natoms}} = -0.336$

The HMOT calculations indicate that naphthalene has the largest delocalization energy and fulvalene has the smallest delocalization energy.

Molecule	E_π	E_{deloc}	$\frac{E_{\text{deloc}}}{\text{atom}}$
Napthalene	-13.683	-3.683	-0.368
Azulene	-13.364	-3.364	-0.336
Fulvalene	-12.799	-2.799	-0.280

The enthalpies of formation are available for naphthalene and azulene and are 150 and 280 kJ/mol, respectively. Thus the rudimentary Huckel calculation is consistent with the thermodynamic data.